**Pushdown Automata - Exercise**

Problem:

Solution:

First, we examine the kinds of words produced by this set. One way to do that is to tabulate the different values of n, m, and k and list the corresponding words for the different values.

n	m	k	w
0	0	0	λ
0	1	2	bcc
1	0	1	ac
1	1	3	abccc
1	2	5	abbccccc
			...

We see that for each a in the word, there is a c produced. For each b in the word, there are two b's. Also, a's, b's, and c's appear in that sequence; i.e., cccba is not accepted.

Open JFLAP and click on *Grammar*. Notice that the resulting window has a LHS column and a RHS column. Each row refers to one rule in the context-free grammar to be created. Using S as the start symbol, fill the first row with S → aSc like so:
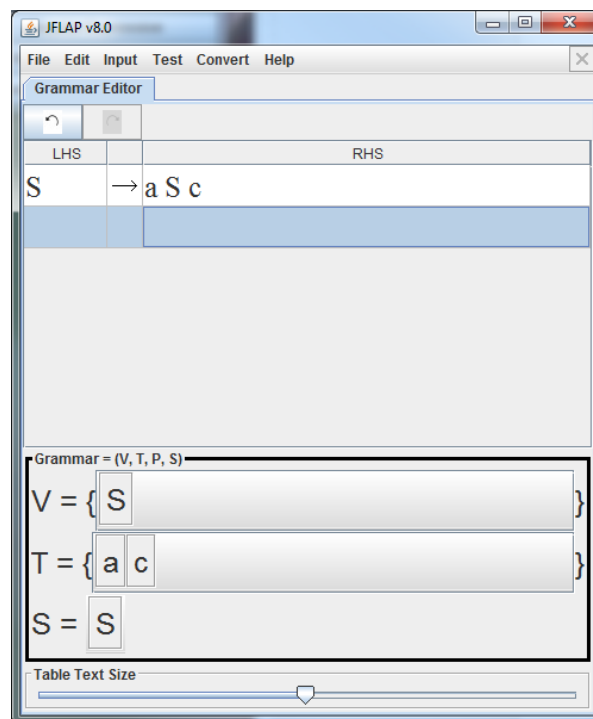
The S in the RHS allows the rule to become recursive. This rule states that for every a created, there is a c at the end of the word created. Next, we introduce a production rule to allow b's to be created. Note that once b's are being produced, we cannot create any more a's. We do this by adding a second rule, S → A.
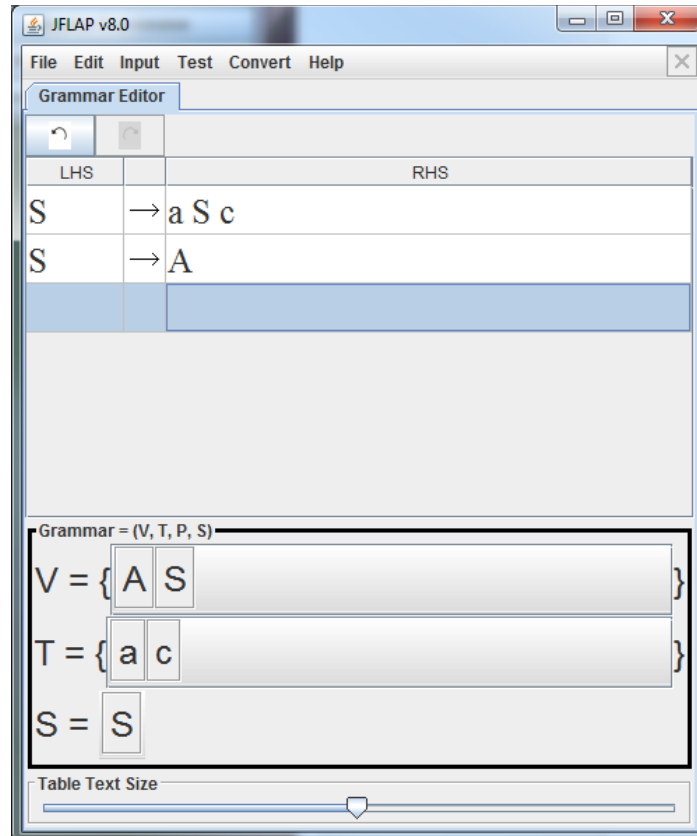
Next, we work on letting b's be created making sure that there are two c's for every b, A → bAcc. This rule is also recursive allowing an infinite number of b's to be created.
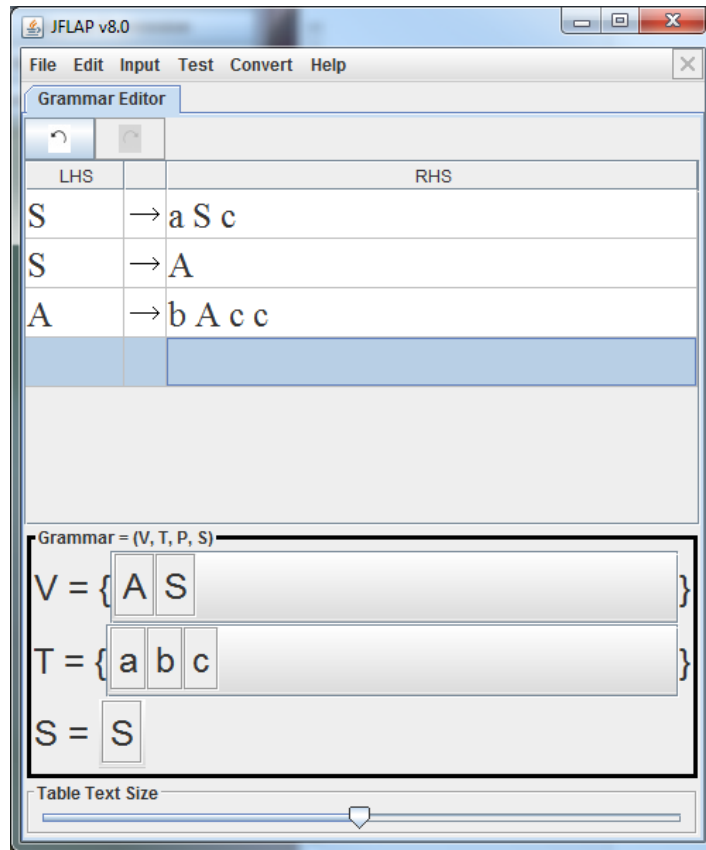
Last, we add a rule to terminate the derivation, A → λ.
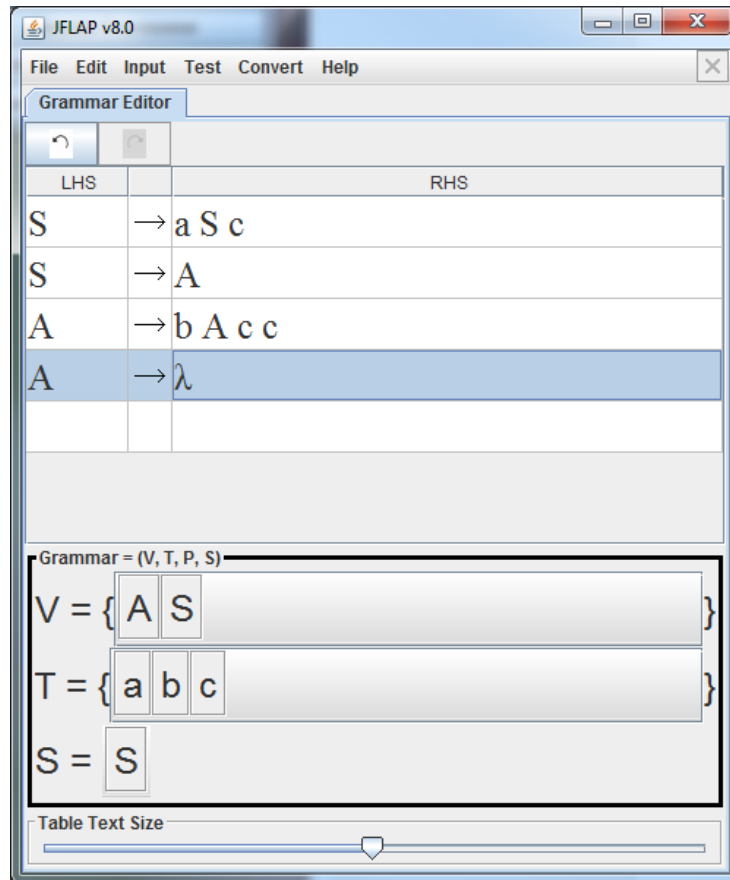
That completes the grammar. Next, we test for grammar type with *Test > Test for Grammar Type*. JFLAP reports that it is a context-free grammar.

Lastly, we may test an input string. Click *Input > Brute Force Parse* and enter *abbccccc* as the input. Click *Complete*. JFLAP reports this string as *accepted*. The brute parse table also shows the 5 derivation levels and the progression from S to the test input.

File   Help

| Grammar Editor | Brute Force Parser |

Input: abbccccc   Set | Change

| Step | Complete | Reset |

Input accepted! Change view to see derivation!

S	→ A
S	→ a S c
A	→ λ
A	→ b A c c

Brute Parse Table

Level	Total Nodes	Current Derivations
1	2	[A, a S c]
2	6	[λ, a A c]
3	8	[a b A c c c]
4	10	[a b b A c c c c c]
5	11	[a b b c c c c c]

Grammar = (V, T, P, S)

V = { A S }

T = { a b c }

S = S

Table Text Size